Effects of Mutual Coupling on Lattice Reduction-Aided Millimeter Wave Hybrid Beamforming

K. Satyanarayana

*University of Southampton & †InterDigital

Co-Authors: Denisa Prisiceanu*, Mohammed El-Hajjar*, Ping-Heng Kuo †, Alain Mourad †, Lajos Hanzo*

ks1r15@soton.ac.uk www.satyanarayana.xyz



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Overview

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mmWave Challenges



I. A. Hemadeh, **K. Satyanarayana**, M. El-Hajjar, L. Hanzo "Millimeter-Wave Communications: Physical Channel Models, Design Considerations, Antenna Constructions and Link-Budget" IEEE Communications Surveys & Tutorials 2018.

mmWave Challenges

- Directional transmission is employed to mitigate the losses
- Conventional MIMO relies heavily on digital signal processing
 - Dedicated RF chains (ADCs) for every antenna element
- Large number of antennas are employed at mmWave frequencies
 - Dedicating RF chains per antenna would incur more cost and complexity
- Analog signal processing along with digital processing, termed hybrid beamforming is a plausible solution [X. Zhang '05]
- State-of-the-art hybrid beamforming designs include fully-connected architecture and sub-array-connected architecture

Fully-Connected Architecture



- The phase shifters of each RF chain are connected to all the transmit antennas
- Number of phase shifters required is equal to $N_t N_t^{RF}$

Dual-Function Hybrid Architecture



Receiver

 $\mathsf{Beamforming} + \mathsf{Diversity}$

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• Number of phase shifters required is equal to $N_t N_{sub}^{RF}$

K. Satyanarayana, et al., "Dual-Function Hybrid Beamforming and Transmit Diversity Aided Millimeter Wave Architecture", IEEE TVT 2017.

Dual-Function Hybrid Architecture

- Beamforming gain is halved for every sub-array partition
- Diversity gain is achieved instead, which is more than the reduction in BF loss for 2 sub-arrays. However, diversity gain diminishes with the increase in the number of sub-arrays



Mutual Coupling

• Transmitting mode



• Receiving mode



System Model

The received signal vector y after hybrid precoding and combining is given by

Received Signal Vector

$$\mathbf{y} = \sqrt{P} \mathbf{W}_{\mathsf{BB}}^{H} \mathbf{W}_{\mathsf{RF}}^{H} \mathbf{H} \mathbf{C} \mathbf{F}_{\mathsf{RF}} \mathbf{F}_{\mathsf{BB}} \mathbf{s} + \mathbf{W}_{\mathsf{BB}}^{H} \mathbf{W}_{\mathsf{RF}}^{H} \mathbf{n}$$

Channel Model

$$\mathbf{H} = \sqrt{\frac{N_r N_t}{N_c N_{\text{ray}}}} \sum_{n_c=1}^{N_c} \sum_{n_{\text{ray}}=1}^{N_{\text{ray}}} \alpha_{n_c}^{n_{\text{ray}}} \mathbf{a}_r(\phi_{n_c}^{n_{\text{ray}}}) \mathbf{a}_t^T(\phi_{n_c}^{n_{\text{ray}}})$$
(2)

Coupling Matrix

$$\mathbf{C} = (Z_A + Z_T) \left(\mathbf{Z} + Z_T \mathbf{I}_{N_t} \right)^{-1}$$
(3)

(1)

where Z_A is the antenna impedance and Z_T is the load impedance.

Achievable Rate

(1/2)



Figure: 64 × 32 MIMO while *d* is 2λ .

K. Satyanarayana, et al., "Millimeter Wave Hybrid Beamforming with DFT-MUB Aided Precoder Codebook Design," in Proc. VTC 2017.

Achievable Rate

(2/2)



Figure: *d* is $\lambda/2$.

Figure: *d* is $\lambda/4$.

Bit Error Ratio (BER)



 At the receiver side, element-based lattice reduction (ELR)-aided detection is employed owing to its low complexity

O. H. Toma and M. El-Hajjar, "Element-based lattice reduction aided K-best detector for large-scale MIMO systems," in Proc. SPAWC 2016.

Bit Error Ratio (BER)

(2/2)



Figure: 8×8 MIMO, ELR-Aided BER

Figure: BER when d is $\lambda/2$, $\lambda/4$.

Conclusions

- Mutual coupling is not always detrimental
- For very small values of *d*, mutual coupling is beneficial, while for large values of *d* mutual coupling has no effect
- For small-to-moderate spacing between antennas, mutual coupling has detrimental effects



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